

Crystal Structure, Phase Transition and Optical Properties of v-PrBO₃

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Abstract: The praseodymium orthoborates λ -PrBO₃ and v-PrBO₃ were synthesized from Pr₆O₁₁ and H₃BO₃ by solid state reaction method at 1200 and 1500°C, respectively. The crystal structure of v-PrBO₃ was refined on the basis of single-crystal X-ray diffraction data. It crystallizes in the triclinic system belonging to space group $P\bar{1}$ with lattice parameters: $a = 0.6302(4)$ nm, $b = 0.6521(4)$ nm and $c = 0.6525(4)$ nm, and $\alpha = 94.312(7)^\circ$, $\beta = 107.335(7)^\circ$, $\gamma = 106.455(7)^\circ$, $V = 0.2417(2)$ nm³, $Z = 4$. The phase transition process from λ -PrBO₃ to v-PrBO₃ was also investigated. The optical band gaps of λ -PrBO₃ and v-PrBO₃ are both determined to be about 4.96 eV according to the diffuse reflection spectra. There is no emission of Pr³⁺ in the visible range for both of λ -PrBO₃ and v-PrBO₃ under X-ray and UV excitation.

Key words: v-PrBO₃ crystal structure; phase transition; optical properties

Over the last several decades, the rare-earth orthoborates REBO₃ have attracted a lot of attention owing to their extraordinary optical properties such as vacuum ultraviolet transparency and exceptional optical damage threshold^[1-2]. It is well known that REBO₃ exhibits the related structure types as the three forms of CaCO₃, *i.e.*, aragonite, vaterite, and calcite^[3]. RE³⁺ adopt different coordination features depending on the size of the rare earth cations^[4], but not with the above three forms at the same time. Most types of REBO₃ are designated with Greek letters in accordance with the nomenclature of Meyer^[5-6]. In general, compounds containing larger ions (La-Nd, Sm, Eu), exhibit the aragonite-type structure (λ -REBO₃) at low temperature^[3, 5], then transform to H-REBO₃ (RE=La, Ce, Nd)^[7] and v-REBO₃ (RE=Ce-Nd, Sm-Dy)^[4-5, 8] at high temperature. However, compounds containing smaller ions exist as a low-temperature modification π -REBO₃ (RE=Y, Nd, Sm-Lu)^[1, 3, 9-10] and a high-temperature modification μ -REBO₃ (RE=Y, Sm-Gd, Dy-Lu)^[1, 10]. Although the high-temperature phases are different, they all exhibit low symmetry. For the smallest ion, ScBO₃ forms the calcite-type structure (β -REBO₃)^[3, 11]. There are some other types of REBO₃ (RE=Er-Lu) which also adopt the same structure at low temperature. Additionally, the orthoborate phases χ -REBO₃ (RE=Dy and Er), which contain the new non-cyclic [B₃O₉]⁹⁻ anion, were synthesized under high-pressure condition by Huppertz, *et al.*^[12], considered

to be intermediates between the low-temperature (π) and high-temperature (μ) polymorphs.

Due to the possible usage for fast scintillators, the Pr³⁺-doped scintillators have attracted the attention of researchers recently, such as Pr³⁺-doped single crystal hosts (Y₃Al₅O₁₂, YAlO₃ and Y₂SiO₅)^[13-14]. This is because that the Pr³⁺ ion can show even faster 5d-4f luminescence shifted by about 1.5 eV towards higher energies with respect to 5d-4f emission of Ce³⁺^[15].

In 1961, Levin, *et al.*^[3] reported the phase transitions of REBO₃ (RE=La, Sm, Nd), which occurred at 1488, 1090 and 1285°C, respectively. The high temperature forms NdBO₃ and SmBO₃ are similar but different from LaBO₃. For the case of PrBO₃, there are few reports on phase transition process. According to previous studies^[2, 6, 16-17], PrBO₃ mainly has two phases: the aragonite phase λ -PrBO₃ (low temperature, LT) and the triclinic phase v-PrBO₃ (high temperature, HT). The two phases exhibit different structures and densities, and the crystal structure determination of λ -PrBO₃ from single crystals obtained through high-pressure and high-temperature synthesis method was reported in 2010^[16]. However, the detailed crystal structure of v-PrBO₃ is still unknown besides the cell parameters of v-PrBO₃ reported by Meyer^[6]. What's more, there is no report about the phase transition and optical properties of PrBO₃. In the present work, we focus on the investigation of the crystal structure of v-PrBO₃, phase

transformation from λ -PrBO₃ (LT) to v -PrBO₃ (HT), as well as its optical properties.

1 Experiment

The λ -PrBO₃ (LT) and v -PrBO₃ (HT) samples were both prepared by solid-state reaction in the muffle furnace. The starting materials were Pr₆O₁₁ (99.99%) and H₃BO₃ (99.99%). A stoichiometric mixture of the starting materials (with 10mol% excess of boric acid to compensate for its evaporation loss during heating) was ground in agate mortar. Then the mixed powders were loaded into platinum crucibles, and calcined in the furnace within air atmosphere at different temperatures. The λ -PrBO₃ (LT) sample was obtained at 1200°C for 12 h, and the v -PrBO₃ (HT) sample was obtained at 1500°C for 5 h. Both powder samples were green. But there are some single crystals in powder v -PrBO₃ (HT) sample.

The powder X-ray diffraction data for λ -PrBO₃ (LT) were collected at ambient temperature in air with a HUBER Imaging Plate Guinier camera G670 [S] (CuK α 1 radiation, $\lambda = 0.154056$ nm, Ge monochromator). The 2θ range of all the data sets is from 5° to 100° with a step of 0.005°.

Single crystal X-ray diffraction data for v -PrBO₃ (HT) were collected with CCD area detector (Mo K α radiation, $\lambda = 0.071073$ nm) at 293(2) K in the range of $3.31^\circ < \theta < 24.98^\circ$ using ω scan. Absorption correction was performed with a multi-scan procedure. The crystal structure refinement was performed by a full-matrix least-squares procedure within the SHELXS97 (Sheldrick, 1990)^[18]. For crystal structure presentation the program Diamond 3.0 was used^[19].

The Fourier transform infrared (FT-IR) spectra of v -PrBO₃ were recorded at room temperature in the range of 400–1600 cm⁻¹ with a Spectrum 100 Optical (Perkin-Elmer).

The diffuse reflectance spectra of the samples were measured at room temperature by a Perkin Elmer LS 50B spectrophotometer equipped with a Xe flash lamp. The reflection spectra were calibrated with the reflection of black felt (reflection 3%) and white barium sulfate (BaSO₄, reflection~100%) in the wavelength region of 200–900 nm.

2 Results and Discussion

2.1 Phase transformation and the structure of the v -PrBO₃

Crystal data for v -PrBO₃: Triclinic, space group $P\bar{1}$ (no. 2), $a = 0.6302$ (4) nm, $b = 0.6521$ (4) nm and $c =$

0.6525 (4) nm, and $\alpha = 94.312(7)^\circ$, $\beta = 107.335(7)^\circ$, $\gamma = 106.455(7)^\circ$, $V = 0.2417(2)$ nm³, $Z = 4$, $M_r = 199.72$, $D_{\text{calcd}} = 5.489$ g/cm³. A total of 1137 data were collected and merged to give 783 unique reflections ($R_{\text{int}} = 0.041$) of which 624 were considered to be observed [$F^2 > 2\sigma(F^2)$]. Final $R_1 = 0.046$, $wR_2 = 0.121$, S (goodness of fit) = 0.98 were obtained for all the data. It confirms that the lattice parameters decrease regularly from Pr, Sm to Dy, along with the size of the cations^[4, 6]. Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ($\times 10^{-2}$ nm²) of v -PrBO₃ are shown in Table 1. For the light atoms of O and B isotropic displacement parameters are used. Important distances (nm) and angles (°) of v -PrBO₃ are given in Table S1. In the structure of v -PrBO₃, the Pr atoms are coordinated by eight O atoms, and the B atoms are in a threefold planar coordination by three O atoms. Figure 1 is the perspective view of the structure of v -PrBO₃ with distorted PrO₈ dodecahedron with Pr–O distances in the range of 0.2297 (11) to 0.2654 (12) nm. Each PrO₈ shares edges with four neighbors to build infinite double chains along the [110] direction. The BO₃ groups are regular, with average B–O distances in the range of 0.135(2) to 0.139(2) nm and O–B–O angles in the range of 116.3 (15)–126.0 (16)°.

The powder X-ray diffraction pattern of λ -PrBO₃ (Fig. S1) confirms the previous study since all diffractions peaks can be readily indexed to the pure orthorhombic-aragonite phase of PrBO₃ (ICSD# 421745) with the cell parameters $a = 0.81419$ nm, $b = 0.57776$ nm, $c = 0.50692$ nm, $V = 0.2385$ nm³. As described by Haberer, *et al*^[16], the aragonite PrBO₃ crystallizes in the orthorhombic Pnma space group with the structure composing of PrO₉ polyhedra and trigonal BO₃ groups. Each PrO₉ polyhedron shares edges with six other PrO₉ polyhedra and three BO₃ triangles. In addition, each BO₃ triangle shares edges with three PrO₉ polyhedra at the same time. By comparison of

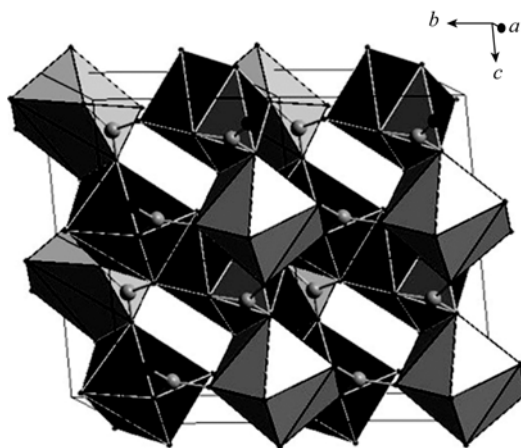


Fig. 1 Crystal structure of v -PrBO₃
Grey and black polyhedra contain atoms Pr1 and Pr2, respectively

Table 1 Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ($\times 10^{-2}$, nm²) of single crystal ν -PrBO₃

Atom	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
Pr1	0.05468 (16)	0.83915 (14)	0.26610 (14)	0.0070 (3)
Pr2	0.44039 (16)	0.71637 (13)	−0.19427 (14)	0.0061 (3)
O1	0.088 (2)	0.8619 (18)	−0.3573 (19)	0.008 (3)*
O2	0.376 (2)	0.8827 (17)	0.1295 (17)	0.004 (2)*
O3	0.035 (2)	0.5314 (18)	−0.2317 (18)	0.008 (3)*
O4	−0.147 (2)	0.787 (2)	−0.134 (2)	0.014 (3)*
O5	0.452 (2)	0.7627 (19)	0.4623 (19)	0.011 (3)*
O6	0.625 (2)	0.6681 (18)	0.1987 (18)	0.008 (2)*
B1	0.495 (3)	0.774 (3)	0.273 (3)	0.007 (4)*
B2	−0.018 (3)	0.716 (3)	−0.244 (3)	0.004 (4)*

Anisotropic atomic displacement parameters ($\times 10^{-4}$, nm ²)						
Atom	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Pr1	0.80 (6)	0.49 (5)	1.03 (6)	0.30 (4)	0.50 (4)	0.32 (4)
Pr2	0.65 (6)	0.35 (5)	0.98 (6)	0.18 (4)	0.42 (4)	0.24 (4)

* isotropic refined atoms

the two modifications, it is obvious that the Pr atoms in the high temperature phase has less coordination number of O than the low temperature phase, and each polyhedron share only 4 edges while 6 edges shared in the low temperature modification. This leads to the obvious changes of the lattice parameters.

According to the discussion above, it is possible that PrBO₃ compound exists in two different phases, *i.e.*, aragonite and triclinic phases. Since there are few reports on the structure phase transition process, it is more worth of notice. In order to study the relationship between the two phases, the sample λ -PrBO₃ synthesized at 1200°C were annealed at 1200°C, 1300°C, 1400°C and 1450°C in air for 5 h, respectively. The results (Fig. 2) turn out that the phase transition point occurs around 1450°C. Since the transition between the two structure modifications did not follow group-subgroup relationship, it may be concluded that the phase transition is first order with reconstructive manner. The detailed mechanism of phase transition of PrBO₃ will be further investigated and published elsewhere.

2.2 FT-IR spectroscopy of ν -PrBO₃

To ascertain the structure of samples, corresponding FT-IR spectroscopy of samples were investigated. The FT-IR spectrum of ν -PrBO₃ in the range of 400–1600 cm^{−1} is shown in Fig. 3.

According to the previous literatures, for an isolated planar trigonal BO₃ group, there are usually six fundamental modes of vibrations, which are symmetric stretch, ν_1 (non degenerate, 950 cm^{−1}), out of plane bending, ν_2 (non degenerate, 740 cm^{−1}), antisymmetric stretch, ν_3 (doubly degenerate, 1250 cm^{−1}), plane bending, ν_4 (doubly degenerate, 600 cm^{−1})^[20]. The observed vibration frequen-

cies of ν -PrBO₃ are listed in Table S2 with their assignments. The modes of vibrations of ν -PrBO₃ are those typical for the isolated planar ion BO₃ as observed in NdBO₃ and SmBO₃^[7]. Therefore, the result is consistent with its corresponding powder XRD data.

2.3 Diffuse reflection spectra of ν -PrBO₃ and λ -PrBO₃

The diffuse reflection spectrum of ν -PrBO₃ is recorded in the range of 230–700 nm (Fig. 4). The figure exhibits a

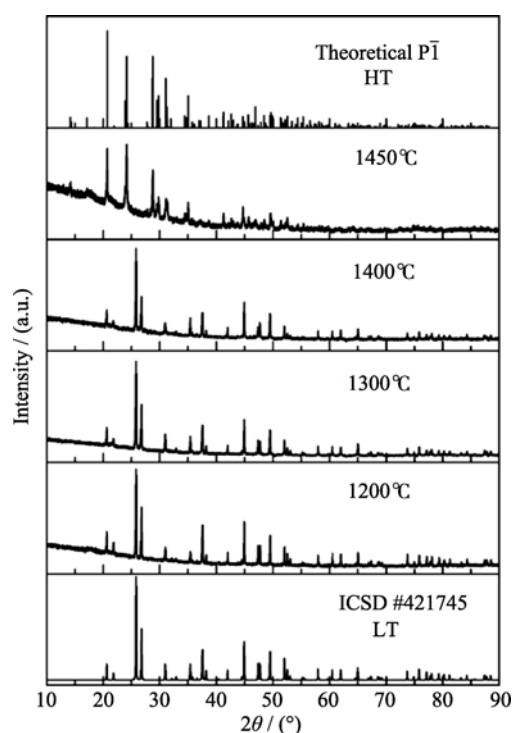


Fig. 2 XRD patterns of λ -PrBO₃ annealed in air at different temperatures

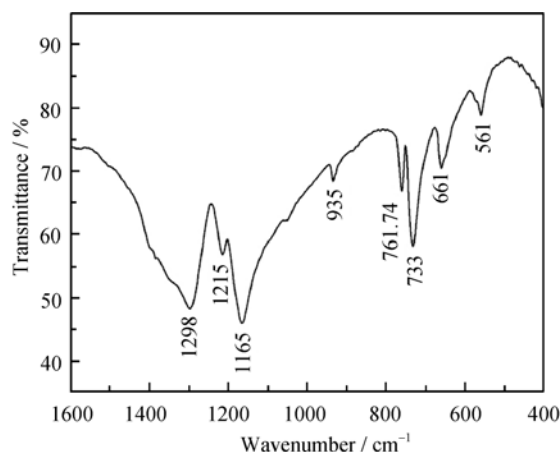


Fig. 3 FT-IR spectrum of v-PrBO₃ in the range of 400–1600 cm⁻¹

drastic drop in the reflection in the UV range around 250 nm (4.96 eV), which defines the optical band gap of v-PrBO₃ host lattice. It shows several absorption lines at long wavelength (*i.e.* low energy) in the range of 448–484 nm as well as 586–598 nm, which are ascribed to the typical f-f transitions from ³H₄ → ³P₂ (~448 nm), ³H₄ → ³P₁ (~474 nm), ³H₄ → ³P₀ (~485 nm) and ³H₄ → ¹D₂ (~598 nm) of Pr³⁺ ions, respectively. The absence of charge transfer band of O²⁻-Pr⁴⁺ rules out the possibility of Pr⁴⁺ in v-PrBO₃, indicating that all the Pr ions in v-PrBO₃ exist in the trivalent state. The daylight color of v-PrBO₃ shows light green as a result of the strong absorption by Pr³⁺ in the visible range of 420–650 nm.

In order to better localize the thresholds for host lattice absorption and the absorption by Pr³⁺, the absorption spectrum of v-PrBO₃ was obtained from the reflection spectrum by using the Kubelka-Munk function^[21]:

$$F(R) = (1 - R)^2 / 2R = K / S$$

Where R , K , S are the reflection, absorption coefficient, and scattering coefficients, respectively. The absorption (K/S) spectrum of v-PrBO₃ derived with the Kubelka-Munk function is shown in the inset of Fig. 4. The value of the optical band gap of v-PrBO₃ is calculated to be about 4.96 eV (*i.e.* 250 nm) by extrapolating the Kubelka-Munk function to $K/S = 0$.

Figure 5 shows diffuse reflection spectrum of λ-PrBO₃ under the same conditions as v-PrBO₃. It shows no obvious change compared to v-PrBO₃. The value of optical band gap of λ-PrBO₃ is also around 250 nm (4.96 eV), which is calculated from the absorption spectrum (the inset of Fig. 5).

The X-ray excited luminescence spectrum and photoluminescence spectra of λ-PrBO₃ and v-PrBO₃ were measured. However, no emission of Pr³⁺ in the UV-Vis range were observed in both of the two host lattices, probably due to the compositional quenching caused by high Pr content.

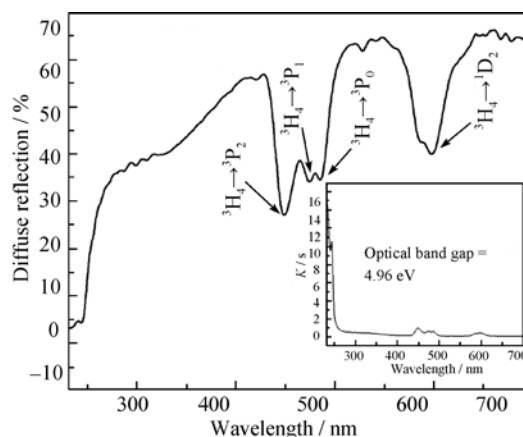


Fig. 4 Diffuse reflection spectrum of v-PrBO₃

Inset shows the absorption spectrum of v-PrBO₃ obtained from the reflection spectrum by using the Kubelka-Munk function

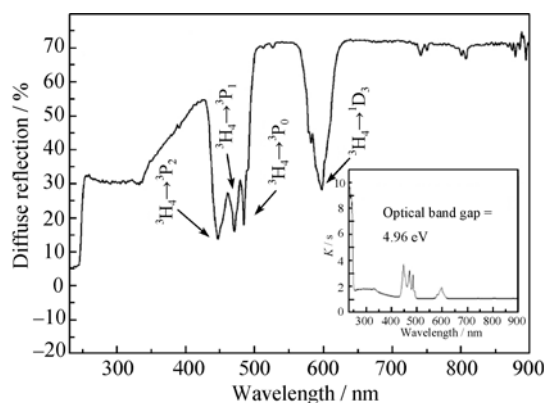


Fig. 5 Diffuse reflection spectrum of λ-PrBO₃

Inset shows the absorption spectrum of λ-PrBO₃ obtained from the reflection spectrum by using the Kubelka-Munk function

3 Conclusions

λ-PrBO₃ and v-PrBO₃ were successfully synthesized by solid state method. The XRD results confirm that the high-temperature phase v-PrBO₃ is isostructural with v-SmBO₃, crystallizes in the triclinic system belonging to space group P $\bar{1}$. According to the XRD results, the phase transition temperature from λ-PrBO₃ to v-PrBO₃ occurs at about 1450°C. The diffuse reflection spectrum of v-PrBO₃ is also studied and its optical band gap is determined to be about 4.96 eV, which has no obvious change compared to λ-PrBO₃. PL and XEL studies of both phases show no emission at visible region.

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ν -PrBO₃ 的晶体结构、相变和光学性质

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摘要: 采用高温固相合成法分别在 1200 和 1500℃ 合成了 λ -PrBO₃ 和 ν -PrBO₃ 样品, 并通过单晶 X 射线衍射确定了 ν -PrBO₃ 的晶体结构。结果表明该结构为三斜晶系, 空间群为 $P\bar{1}$, 晶胞参数为 $a = 0.6302(4)$ nm, $b = 0.6521(4)$ nm, $c = 0.6525(4)$ nm, $\alpha = 94.312(7)^\circ$, $\beta = 107.335(7)^\circ$, $\gamma = 106.455(7)^\circ$, $V = 0.2417(2)$ nm³, $Z = 4$ 。同时研究了从 λ -PrBO₃ 到 ν -PrBO₃ 的相变过程, 并从漫反射光谱得出 λ -PrBO₃ 和 ν -PrBO₃ 的光学带隙均为 4.96 eV。在 X 射线和紫外激发下, 均未观测到 λ -PrBO₃ 和 ν -PrBO₃ 样品在紫外可见波长范围内的 Pr³⁺ 特征发光。

关键词: ν -PrBO₃ 晶体结构; 相变; 光学性质

中图分类号: O78

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Supporting Information

Crystal Structure, Phase Transition and Optical Properties of ν -PrBO₃

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Table S1 Important distances ($\times 10^{-1}$, nm) and angles ($^{\circ}$) of single crystal ν -PrBO₃

Atoms	Distance and angle	Atoms	Distance and angle
Pr1—O3i	2.297 (11)	Pr2—O5v	2.304 (11)
Pr1—O1ii	2.392 (11)	Pr2—O4vi	2.414 (13)
Pr1—O2	2.398 (11)	Pr2—O6vii	2.419 (11)
Pr1—O1iii	2.470 (12)	Pr2—O3	2.422 (11)
Pr1—O4	2.487 (12)	Pr2—O2viii	2.486 (11)
Pr1—O6iv	2.505 (12)	Pr2—O2	2.496 (11)
Pr1—O4iii	2.615 (12)	Pr2—O6	2.565 (11)
Pr1—O5	2.654 (12)	Pr2—O1	2.627 (12)
B1—O5	1.35 (2)	B2—O1	1.39 (2)
B1—O2	1.39 (2)	B2—O3	1.34 (2)
B1—O6	1.37 (2)	B2—O4	1.38 (2)
O5—B1—O6	126.0 (16)	O3—B2—O4	125.9 (15)
O5—B1—O2	116.4 (16)	O3—B2—O1	117.3 (15)
O6—B1—O2	117.1 (15)	O4—B2—O1	116.3 (15)

Symmetry codes: (i) $-x, -y+1, -z$; (ii) $x, y, z+1$; (iii) $-x, -y+2, -z$; (iv) $x-1, y, z$; (v) $x, y, z-1$; (vi) $x+1, y, z$; (vii) $-x+1, -y+1, -z$; (viii) $-x+1, -y+2, -z$; (ix) $-x, -y+2, -z+1$.

Table S2 Observed frequencies of the different vibration modes in ν -PrBO₃

Band/cm ⁻¹	Assignment $\nu(\text{B-O})$ in BO ₃
1298	ν_3
1215	ν_3
1165	ν_3
935	ν_1
762	ν_2
733	ν_2
661	ν_4
561	ν_4

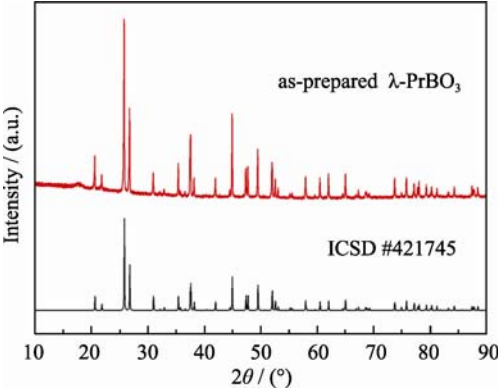


Fig. S1 The powder X-ray diffraction pattern of λ -PrBO₃